

Exploring the transition behavior of nodes in temporal networks based on dynamic community detection

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Abstract

Community detection and community evolution tracking are two important tasks in dynamic complex network analysis. Recently, a variety of models and methods have been proposed for detecting the community structure and analyzing their evolution. However, all these methods are only committed to improving the performance of community detection or identifying evolutionary events, ignoring the internal relevance between the structure of each snapshot of the dynamic network and the evolution pattern of communities, especially the structural features of nodes and their dynamic transition behavior. To cope with this problem, we firstly conduct experiments on 15 real-world dynamic networks to explore the transition behavior of nodes in dynamic networks, which is one of the most influential evolutionary patterns in temporal community detection. Firstly, we obtain the temporal community structure based on very successful temporal community detection methods. Secondly, we extract features of nodes based on the structure of the dynamic network, and take the community transition behavior of nodes as the binary classification problem. Finally, we use the decision tree to find the node-level features that have a general impact on node transition. Experiments indicate that the degree and average neighbor degree of nodes have the most common indispensable impact on the node transition

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behavior, which are very helpful for modeling dynamic complex networks in future.

Keywords: dynamic complex network, node transition, node-level feature, binary classification, average neighbor degree

1. Introduction

Complex network analysis [1, 2] has received increasing attention from researchers in different fields, including computer science, social science, and physical science [3, 4, 5]. Complex networks always consist of nodes and edges, which represent the objects and the interactions between the objects, respectively. For example, in a social network, nodes could be the social accounts and edges represent the following or followed relationships between accounts. As one of the most important and powerful data structures, analyzing and modeling complex networks can be used for many missions, such as social interaction pattern analysis, social recommendation and protein functional modules recognition. As the most fundamental tasks in complex networks, node identification, link prediction and information dissemination have been widely studied and concerned. In addition, community detection is also one of the most significant tasks, which is usually defined as identifying tightly linked subgraphs from complex networks and benefiting from other tasks.

In general, detecting community structures can help us recognize meaningful modules of a network. A variety of works for community detection have been developed, such as modularity-based methods [6], model-based methods [7, 8] and random walk-based methods [9, 10, 11], where comprehensive surveys can be seen in [12, 13]. However, all these methods assume that the target network is static, that is, the network structure is invariant. Virtually, the network structure varies over time, i.e. dynamic networks. More specifically, in a dynamic network, the nodes may birth or death with time and links between two nodes may appear or disappear. For dynamic network modeling, we usually reply to it as a series of snapshots or slices, each of which can be regarded as a static

network. From the perspective of community detection, compared with static networks, detecting the dynamic community poses new challenges [14], among which, how to fuse consecutive snapshot networks to improve performance of community detection and how to describe the evolution of communities are the most important.

Take a co-author network as an example, just as shown in Fig. 1, we show two snapshots of the dynamic network based on the DBLP data [15]. The nodes and edges are the authors and their cooperative relationship, and nodes with the same color represent the same community to which they belong. These three communities are the authors from data mining, database and machine learning, respectively. From the last snapshot to the next, a very important phenomenon is that the research field of some nodes has changed, for example, an author from the database joins into the data mining with the time going by and varying of the network. This is a critical behavior of community detection in dynamic networks, i.e. the transition behavior of nodes, which is the most widely considered dynamic pattern and also is our concern in this paper.

In recent years, more and more attention has been paid to dynamic community detection and different methods have been proposed, including two-step methods, evolutionary clustering methods and model-based methods. Two-step based methods [16, 17] usually apply a static community detection algorithm to each snapshot, and then perform community matching step at adjacent time slices. This kind of methods is not accurate enough because data in the real world is often noisy. Moreover, such a two-step process usually results in unstable community structures and consequentially, unwarranted community evolution [15]. Evolutionary clustering is firstly devoted to clustering the stream data and has been developed for dynamic community detection, the previous or historical network or community information are integrated into the community detection in following subsequent network snapshots, such as the evolutionary spectral clustering, dynamic non-negative matrix factorization and multi-objective evolutionary clustering [18, 19], this type of methods is still the most widely studied and used. The model-based methods [20, 21] usually define

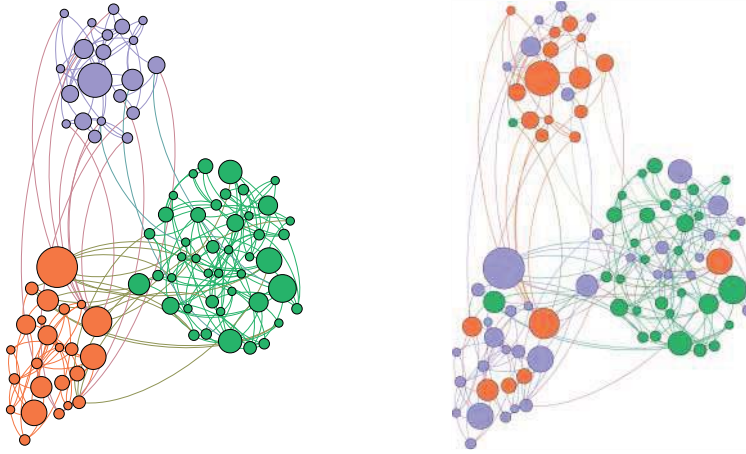


Figure 1: A co-author network with two snapshots. The left figure is the co-authorship of three communities in the previous snapshot, corresponding to the data mining (green), database (blue) and machine learning (orange), while the right figure shows the community assignment changes in the next snapshot.

a series of network generation mechanisms to reconstruct the dynamic complex network and analyze the evolution of communities, such as the dynamic stochastic block model DSBM [15], which denoted the dynamic pattern based on the classic SBM and transforming community detection and evolution into
60 on the classic SBM and transforming community detection and evolution into the parameter estimation. On the whole, the model-based methods have very high computational complexity.

As we all know, all the existing methods for dynamic community detection are focusing on the performance of community detection and the evolutionary
65 patterns or events, while ignoring the internal relevance between the structure varying of dynamic network and the evolution pattern of communities. Therefore, we are interested in, how the structural information of nodes affects the community transitions. In other words, community evolution is usually driven by node transition, and the relationship between the transition behavior and
70 the local varying of nodes is our concern. Although some model-based methods (e.g. [22, 23]) use the degree of nodes to improve the accuracy of community detection, these methods only make the node distribution within a community following the power law and do not reveal the relationship between nodes de-

gree and community evolution. As we have discussed, what kind of nodes are
75 more likely to transfer their communities? Are there more statistical features
related to the transfer behavior of nodes? Which is the most important feature?
We believe that this could help us design more suitable models for community
discovery in dynamic networks.

Our motivation is to explore which local structure information or features of
80 the node has important impact on the transition behavior of nodes in dynamic
networks, and which structural feature has a larger influence and which one has
a small impact. So in this paper, for a given dynamic network, we firstly obtain
its community structure based on three very successful temporal community
detection methods. Then, we extract the ten features of nodes based on the
85 structure of the previous snapshot network, and take the community transition
behavior of nodes as the binary classification problem. In detail, we use the
decision tree as the classification model to find the node-level features that have
a general impact on node transition and analyze the community evolution on all
the snapshots of the dynamic network. We take the framework on 15 real-world
90 dynamic networks shows that the degree and average neighbor degree of nodes
are the most two important features impacting on the node transition behavior.
We believe that this is very helpful for modeling dynamic complex networks in
future. The specific contributions of this paper are as follows:

- As far as we know, this paper is the first exploration of the problem that
95 what kind of nodes is more likely to transfer its community, it is the most
important behavior in dynamic networks.
- We extract the community features of the nodes belonging and features
of the nodes themselves, and treat the node’s community transition as a
binary classification problem, then use these features to classify whether
100 the nodes are transferred or not.
- We find that the important common feature of the node’s community
transition is node’s average neighbor degree and node’s degree. And node’s

average neighbor degree is even more important than node’s degree, which is inconsistent with our previous understanding.

105 2. Related Work

Community detection is a fundamental task in complex network analysis, which can offer insight into the network formation mechanism and prediction [13, 24].

There have been a variety of methods proposed for community detection, including modularity optimization methods, spectral clustering methods and model-based methods. For example, Liu et al. [25] proposed a modularity optimization method using simulated annealing with a k-means iterative procedure to realize the model selection, which outperforms most of the similarity methods. Some other methods [26] detect clusters of networks by utilizing the spectral properties of the graph, but when the network is sparse, the eigenvalues of the community-related eigenvectors are not disparate, which may make spectral clustering unstable. Krzakala et al. [27] proposed a spectral algorithm based on a non-backtracking walk to solve this problem on directed networks. Karrer et al. [7] proposed a model-based method called the degree corrected stochastic block model, in which nodes in the same community can have heterogeneous degrees. That is in line with real-world data. The detailed review can be seen in [13]. However, all these methods are only designed for static networks without considering the temporal information.

Dynamic community detection needs to solve two key sub-problems. One is detecting community structure of each snapshot, and the other is matching communities across consecutive time slices or tracking community evolution. Most previous studies have addressed these two issues separately.

For the first problem, previous works can be divided into two-step methods, evolutionary clustering and model-based methods. The two-step approaches solve this problem by performing a static community detection method on each snapshot and then matching communities between consecutive snapshots. Taje-

una et al. [28] proposed a two-step method, which uses a similarity measure that involves the global temporal aspect of the network under investigation to match the communities in different time slices. Evolutionary clustering introduces the
135 community division information from previous snapshots when performing the community detection approach to the current snapshot [19]. TILES [29] is a state-of-the-art evolutionary clustering method, which dynamically recomputes community membership of nodes whenever a new interaction takes place. This strategy makes TILES fit for large networks and its accuracy is higher than
140 most existing algorithms. Model-based methods, like dynamic stochastic block model [15], considering the dynamic network from the perspective of generating model, the mechanism of the network is constructed and the community structures are obtained by parameter estimation [30, 31].

Meanwhile, for community evolution, this exciting work [32] summarizes
145 community evolution into identifying some events, and then uses these events to carry out community and node evolution behavior. Palla et al. [16] is the first to give the definition of six community evolution events, including birth, death, merging, splitting, growth and contraction. They first used a clique percolation method to detect communities in each snapshot, then matched community evo-
150 lution events and analyzed community evolutionary and node behavior prediction in consecutive snapshots by defining an auto-correlation function. Greene et al. [33] proposed a standard dynamic network data set based on community evolution events, which has been widely used in dynamic community detection. Asur et al. [34] not only define five community events, but also define four
155 node-level events, including appear, disappear, join and leave, to capture the influence of the behavior of nodes on communities. But the dynamic behaviors of different nodes are complex, and they have different effects on the community. However, these works did not take into account that the evolutionary behaviors of different nodes are distinguishing, and the impact on the community is also
160 different.

Some researchers have realized that the node behavior is the driving force of community evolution, and community evolution plays a key role in temporal

community detection. Therefore, some previous work has begun to use node structural features to enhance dynamic community detection [33].

165 In addition, there are some researchers trying to use node embedding model dynamic network [35]. They generally treat node embedding vectors as node structural features and then use the node embedding vectors to enhance dynamic community detection. However, this makes the node features unexplainable, as a result, we cannot understand how node structural features affect community-
 170 level evolution. Meanwhile, Yin et al. [36] used node average neighbor degree to enhance link prediction, but they did not discuss the general influence of node average neighbor degree on real-world data sets.

3. Proposed Framework

In this section, we introduce how to find the most critical structural features that affect the transition behavior of nodes across the snapshots.

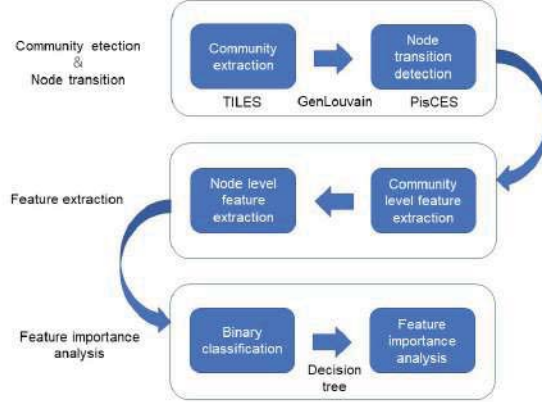


Figure 2: Framework schematic

175 The proposed framework is depicted in Fig. 2, first of all, we use some temporal community detection methods to detect node community membership and node transition behaviors. Then, we extract the structural features of nodes and use them as classification features. We assume that the node community
 180 transition is only related to node structural features in the current snapshot,

so we split snapshots in a network into adjacent snapshot pairs, and besides, different snapshot pairs in the same network are independent. We then treat the node community transition as a binary classification problem. For example, if a node i transfers its community membership between consecutive snapshots, then it is labeled $L_i = 1$. Finally, the most critical node structure features that affect the node community transition are analyzed.

To show the consistency of our proposed framework and experimental results, we select three popular and successful approaches for dynamic community detection: (1) TILES [29], which belongs to the evolutionary clustering framework. It effectively uses the network structure at time t and the community structure at the previous moment to detect the community at time t , which better community detection performance and lower computational complexity; (2) GenLouvain [37], which is a fast algorithm of modularity optimization for time-dependent networks. It generalizes the determination of community structure via quality functions to dynamic networks and could discover some important dynamic patterns; (3) PisCES [38], which is a global community detection method based on discovering persistent communities by eigenvector smoothing and combining information across a series of snapshots. It is also data-driven and can reveal dense communities that persist, merge, and diverge over time.

3.1. Notations and Definitions

We use $\mathcal{G} = (\mathcal{V}, \mathcal{E})$ to denote a collection of the dynamic network, where \mathcal{V} is the set of nodes and \mathcal{E} is the set of edges of the dynamic network. We fix the number of nodes in the network. Therefore, the nodes of the dynamic network do not change over time, which means that the size of the nodes collection $|\mathcal{V}| = N$ is a constant in the dynamic network. We use the changes in edges to represent the changes in the network. Therefore, a new node joins in the network can be treated as an isolated node with links to other nodes. Thus, the size of edges changes over time. We use $|\mathcal{E}|$ to represent the size of edges in the whole network and $|\mathcal{E}^t|$ to represent the size of edges in the t -th snapshot. Furthermore, we also use $\mathcal{G} = (\mathcal{G}^1, \mathcal{G}^2, \dots, \mathcal{G}^T)$ to represent a dynamic network,

where T representing the number of network snapshots and \mathcal{G}^t representing the t -th snapshot in the network. We then use $\mathcal{C}^t = (c_1^t, \dots, c_N^t)$ to represent the nodes community membership at snapshot t . More specifically, $c_i^t = k$ represents node i belong to community k at snapshot t .

215 3.2. Community Detection and Node Transition Detection

For the first step in our framework, we need to detect community structures and node transition behaviors from network triplet data. We select the following three methods, namely, TILES [29], GenLouvain [37] and PisCES [38].

- 220 • TILES [29] can solve both problems at the same time. TILES is a state-of-the-art evolutionary community detection algorithm. It proceeds to analyze an interactive stream: when a new link is generated, TILES uses a label propagation procedure to diffuse the changes to the node surroundings and adjust the neighborhood community membership. A node in TILES can belong to a community with two levels, i.e. peripheral level
225 and core level. A node is a core node if it involves at least a triangle with other nodes in the same community, and it is a peripheral node if it is a one-hop neighbor of the core node. Only core nodes are allowed to spread community membership to their neighbors.
- 230 • GenLouvain [37] proposes a multislice generalization of modularity inspired by the equivalence between the modularity quality function (with a resolution parameter) and stability of communities under Laplacian dynamics. It can be used for multiple scales, time-dependent and multiplex networks. This metric can be effectively learned by any modularity optimization method.
- 235 • PisCES [38] extends the spectral clustering for dynamic networks through eigenvector smoothing, then it proposes an objective function based on the series of eigenvectors across the snapshots, and finally, an iterative algorithm is proposed for detecting the temporal communities.

It should be noted that TILES generates overlapping communities. It be-
 240 lieves that overlapping communities represent different spheres of the social
 world of an individual. This brings us some troubles, because if a node belongs
 to different communities at the same time slice, how can we determine that this
 node changes its community membership in the next time slice? We believe that
 a node will transfer its community membership when it joins a new community,
 245 because a new community can represent a new social hub or new interest of
 an individual. Feature selection has always been an active and widely accepted
 method for enhancing the quality of data in machine learning and data mining.

Algorithm 1 Feature extraction

Input: A sequence of undirected graphs $\mathcal{G} = \mathcal{G}^1, \dots, \mathcal{G}^T$ and the community
 assignment $\mathcal{C} = \mathcal{C}^1, \dots, \mathcal{C}^T$

Output: Nodes feature set F and nodes label set L

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1: for every graph  $\mathcal{G}^t$  where  $t \neq T$  do
2:   for every community  $\mathcal{C}_i^t$  in  $\mathcal{C}^t$  do
3:     Calculate community level features  $F_c$ 
4:     for every node  $i$  in community  $\mathcal{C}_i^t$  do
5:       Calculate node level features  $F_n$ 
6:       Compose node  $i$ 's feature sequence  $F = F_c + F_n$ 
7:       if node  $i$  changes its community in  $\mathcal{G}^{t+1}$  then
8:         node  $i$ 's label  $L_i = 1$ 
9:       else
10:        node  $i$ 's label  $L_i = 0$ 
11:      end if
12:    end for
13:  end for
14: end for
```

3.3. Feature Selection and Extraction

250 Considering that the transfer behavior of a node is affected by the community in which it belongs to, we also introduce several community-level features. For example, if an online social group is not active enough, the members of the group will be more likely to join other groups. So we need to take community-level features into consideration, to verify its influence on the node community
255 transition for the empirical evidence. Thus, our node features contain community structural features and node structural features in the network.

We use five community-level features to represent the state of the community in which the node is located, including the number of community nodes, the number of community edges, intra-community edges, inter-community edges
260 and community activities. These features can be considered as higher-level local structural features of nodes. In addition, we use five node features to capture the node lower-level local structural features, including node degree, node average neighbor degree, node closeness centrality and node betweenness centrality. The detailed description of node features is listed in Table 1.

265 The feature extraction algorithm is provided in Algorithm 1. To calculate the node’s features effectively, we calculate community-level features before calculating node features that are part of this community. And after splitting snapshots of a network into snapshot pairs, our feature extraction algorithm can run in parallel. This can make our algorithm suitable for a large scale
270 network.

3.4. Feature Importance Analysis

We use decision tree [39] to solve the binary classification problem. Because a decision tree is a white-box algorithm, it can tell us which feature plays a more important role in the classification mission. Different from artificial neural
275 networks and other black-box algorithms, it can output any information needed during the classification process.

A decision tree is a solution support tool that uses a tree-like graph or model of decisions. Each node of the decision tree is a “test” of the feature

Table 1: Notations and definitions

Symbol	Feature	Description	Definition
$f1$	Community node number	Number of nodes within the community l at time t .	n_l^t
$f2$	Community edge number	Number of edges within the community l at time t .	e_l^t
$f3$	Intra community edges	Ratio of the total number of edges between the nodes inside the community ($e_l^t(in)$) to the number of nodes in the community.	$\frac{e_l^t(in)}{n_l^t}$
$f4$	Inter community edges	Ratio of the total number of edges of nodes connected outside the community ($e_l^t(out)$) to the number of nodes in the community.	$\frac{e_l^t(out)}{n_l^t}$
$f5$	Community activity	Ratio of the total number of connections made in the previous snapshot by the nodes of the community (a_l^t) to the number of nodes in the community.	$\frac{a_l^t}{n_l^t}$
$f6$	Community Conductance	Ratio of the number of edges in the community to the sum of degrees of the nodes in the community.	$\frac{e_l^t}{d_l^t}$
$f7$	Node degree	Sum of links connected to node i at time t .	e_i^t
$f8$	Node average neighbor degree	Average degree of node i 's neighbors, where $N(i)^t$ are the neighbors of node i at time t and e_j^t is the degree of node j which belongs to $N(i)^t$.	$\frac{1}{ N(i)^t } \sum_{j \in N(i)^t} e_j^t$
$f9$	Node closeness centrality	Measuring a node i 's average path length to other nodes in community, where $C_{l,-i}^t$ is a set of all nodes in community l except i at time t and $d(i,j)$ is the distance between node i and j .	$\sum_{j \in C_{l,-i}^t} \frac{C_l^t}{d(i,j)}$
$f10$	Node betweenness centrality	Measuring a node i 's importance in its community connectivity, where σ_{jk} is the total number of shortest paths from node j to node k and $\sigma_{jk}(i)$ is the number of those paths that pass through i	$\sum_{j,k \in C_{l,-i}^t} \frac{\sigma_{jk}(i)}{\sigma_{jk}}$

(e.g. whether a coin flip appears at the head or tail), each branch is the result of the test (e.g. the head and the tail of a coin flip are two branches), and each leaf node is a class label. The path from the root to the leaf represents the classification rule. Decision tree is an efficient algorithm for classification mission. The cost of using a tree is logarithmic, which makes it very fast in large data sets.

We use Gini importance or Mean Decrease in Impurity (MDI) to calculate each feature importance as the total decrease in node impurity [40]. Node impurity like Gini impurity is a computationally efficient approximation to the entropy, which can measure how well a potential split is separating the samples in a decision tree node. Decrease Impurity is defined as below:

$$\Delta i(s, r) = i(r) - p_L i(r_L) - p_R i(r_R), \quad (1)$$

where $i(r)$ is some impurity measure like Gini index, r represents a decision tree node, and r_L and r_R are the children of r . Besides, $p_L = N_{r_L}/N_r$ and $p_R = N_{r_R}/N_r$, where N_r is the number of samples go through node r .

The normalized $\Delta i(s, r)$ for each feature can give us a kind of importance measure, and it is very computationally efficient for large scale data sets.

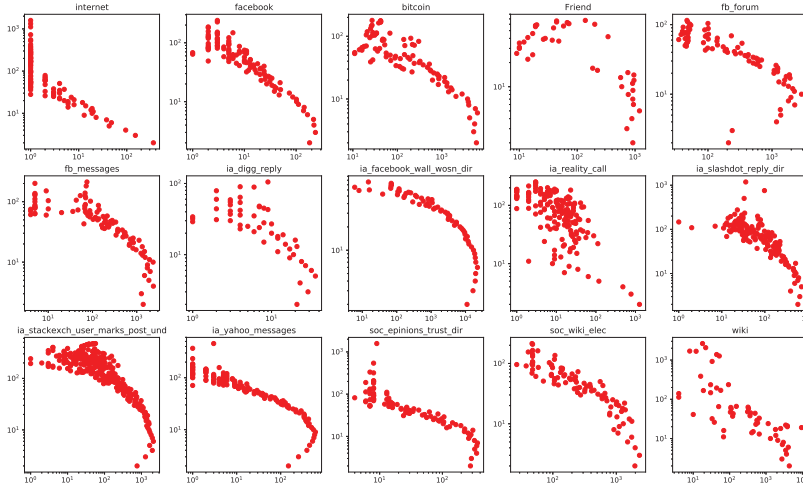


Figure 3: The degree distributions of 15 dynamic networks.

295 4. Experiment

In this section, we first introduce the details of the 15 real-world data sets used throughout this paper. Then we show the binary classification results in 15 data sets and our findings in feature importance experiment, that is, node degree and node average neighbor degree are the two most important structural features for node community transition.

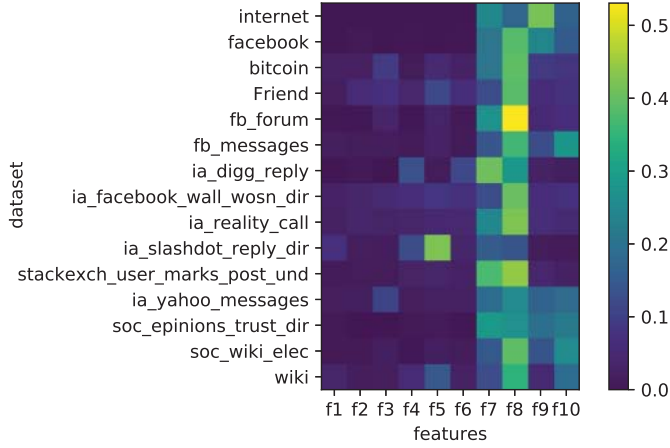


Figure 4: The importance of different node characteristics or features on the dynamic behavior of 15 real dynamic networks based on the TILES [29] method.

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4.1. Real-World Data Sets

The data sets used in the experiment contain different types of networks, for example, *social networks* with social account users as nodes and relationship as links, *friends cell phone call records networks* with phone owners as nodes and phone contacts as links, *who-trust-whom networks* with people as nodes and trust relationships as links and *tech-website answering questions networks* with website account as nodes and answering questions as links. The characteristics of the data sets and their sources are given in Table 2. Figure 3 shows all of the node distributions of our data sets follow a power law.

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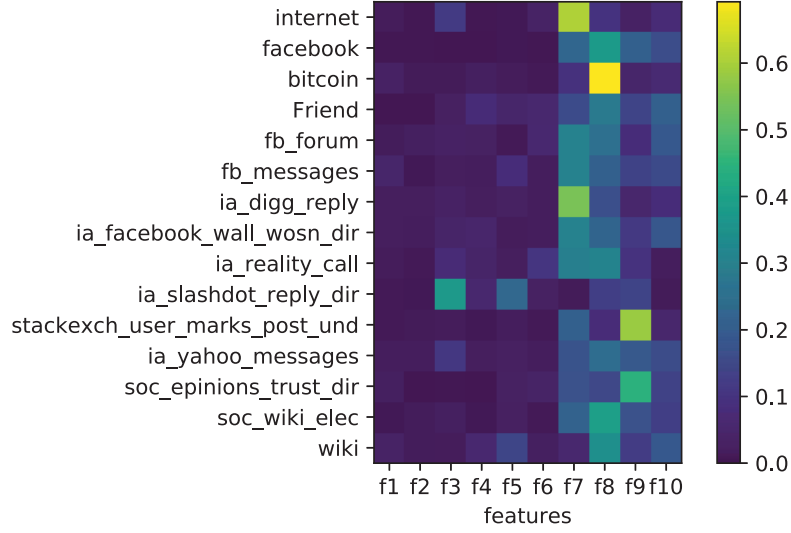


Figure 5: The importance of different node characteristics or features on the dynamic behavior of 15 real dynamic networks based on the GenLouvain [37] method.

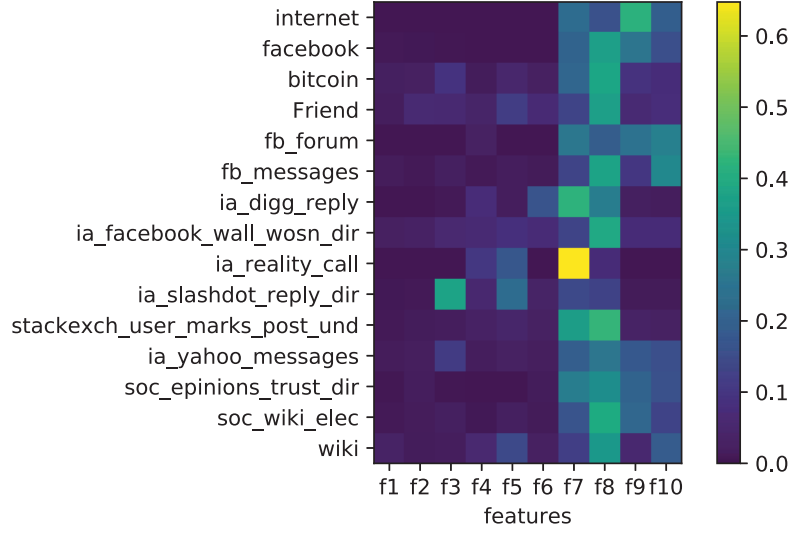


Figure 6: The importance of different node characteristics or features on the dynamic behavior of 15 real dynamic networks based on the PisCES [38] method.

Table 2: Description of data sets

Name	Description	$ \mathcal{V} $	$ \mathcal{E} $
Internet	Internet [41] topology during 04/01/2004 – 04/04/2005.	33936	104824
Facebook	Facebook New Orleans networks [42] friends links during 06/08/2008 – 21/01/2009.	62306	905565
bitcoin	Who-trusts-whom network of people who trade using Bitcoin on Bitcoin OTC [43] during 09/11/2010–19/01/2016.	5881	35592
Friend	Call logs of members of a young-family residential living community adjacent to a major research university in North America [44] during 10/07/2010 – 16/07/2011.	130	60518
fb-forum	The Facebook-like Forum Network [45] during 15/05/2004 – 24/10/2004.	899	33720
fb-messages	The Facebook-like Social Network [45] from an online community for students at University of California during 24/03/2004 – 22/10/2004.	1897	61734
ia-digg-reply	A reply network of the social news website Digg [45] during 29/10/2008 – 13/11/2008.	30397	87627
ia-facebook-wall-wosn-dir	The Facebook friendship graph [45] during 15/05/2004 – 24/10/2004.	44668	876993
ia-reality-call	The MIT Reality mining a small set of human call logs data [45] during 24/09/2004 – 07/01/2005.	6810	52050
ia-slashdot-reply-dir	Reply network of technology website Slashdot [45] during 01/12/2005 – 31/08/2006.	51097	140778
ia-stackexch-user-marks-post	User answering question network of Stack Overflow [45] during 03/10/2008 – 25/11/2011.	545196	1302439
ia-yahoo-messages	The message network in Yahoo [45] with time presented by link sequences.	99303	3179718
soc-opinions-trust-dir	Epinion who-trusts-whom network [45] with time presented by link sequences.	131828	841373
soc-wiki-elec	Wikipedia adminship election data [45] during 14/09/2004 – 05/01/2008.	8271	107071
wiki	The Wikipedia links data [41] during 20/02/2001 – 06/12/2002.	329623	39953145

310 4.2. Feature Importance

We use the decision tree to process the node binary classification mission on 15 real-world data sets. As mentioned before, decision tree is an efficient algorithm for classification, so it is a good choice to execute binary classification in large data sets. Moreover, it allows us to calculate the feature importance in
315 classification mission.

Figures 4, 5 and 6 show the importance of different node characteristics or features on the dynamic behavior of 15 real dynamic networks based on the TILES [29], GenLouvain [37] and PisCES [38], respectively. The results all show that node degree (f7) and node average neighbor degree (f8) are the
320 two generally important features for node community transition on dynamic networks, which means that node degree and node average neighbor degree affect almost all the real-world data sets in community transition. Furthermore, node community activity plays an important role in slashdot reply data, but this feature is not applicable to all other data sets, which means that it does
325 not have a general impact on community transition. Other community-level features, such as the number of community node, have no obvious guarantee against community transition. On the contrary, node-level features, such as node closeness centrality and node betweenness centrality, have a few intense on some data sets like internet, facebook and facebook messages. However, they
330 did not work well on digg reply data or slashdot reply data. It also proves that the node closeness centrality and node betweenness centrality have no general influence on community transition.

Figure 7 shows the bitmaps of node degree in different labels (1 represents nodes who transferred their community, 0 otherwise) on 15 data sets. As we can
335 see, it shows an obvious pattern, that is, all nodes that transfer their communities have a higher degree than nodes that do not transfer their communities. This pattern proves that degree-corrected models like [46, 47, 7] have to be in conformity with the facts. Other features like node community activity, node closeness centrality and node betweenness centrality may play important roles
340 in community transition in some data sets, but not all of them. Just as shown

in Fig. 8, node closeness centrality does not show obvious pattern on all 15 data sets. Even in internet data, which shows the important instance of node closeness centrality, node closeness centrality still does not show significant differences between different labels. Furthermore, we find that the node average
345 neighbor degree also plays an important role, or in other words, it plays a more important role than the node degree in almost all data sets we used. However, just as shown in Fig. 9, although the different labels on each data set are different, the bitmaps do not show an obvious consistent pattern. Through a case study on how the average neighbor degree of nodes affects the migration
350 of a node community, it is found that it is still useful for dynamic community detection or community evolution.

Just as shown in Fig. 10(a), we chose three most representative data sets, namely, stackoverflow (left two columns), Friend (middle two columns) and facebook-wall-wosn (right two columns). The left column in every data set is
355 the degree of nodes to which the nodes of communities have changed. The nodes that transferred their community have a larger degree than the nodes that did not. And as shown in Fig. 10(b), we also chose three most representative data sets, namely, facebook (left two columns), Friend (middle two columns) and facebook-wall-wosn (right two columns). The left column in every data set is
360 the average neighbor degree of nodes that changed communities, which proves that nodes that transferred their communities have a larger average neighbor degree than the nodes that did not.

It is undoubtedly that the node degree can affect node community transition. Obviously, the higher the degree of nodes, the more likely it is to encounter nodes
365 in other communities. And if the average neighbor degree of a node is larger, then the node is more likely to be affected by its neighbors. We will show a real-world case in the next section.

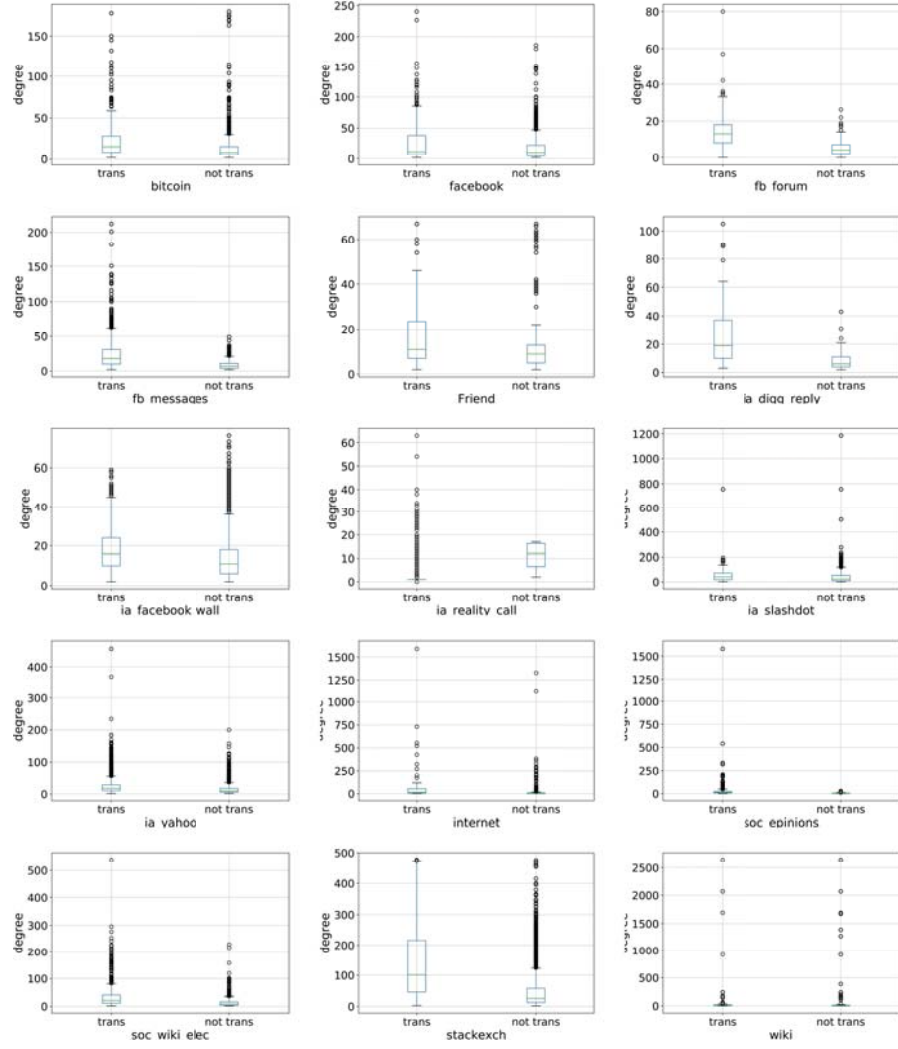


Figure 7: Bitmaps of nodes degree on 15 data sets

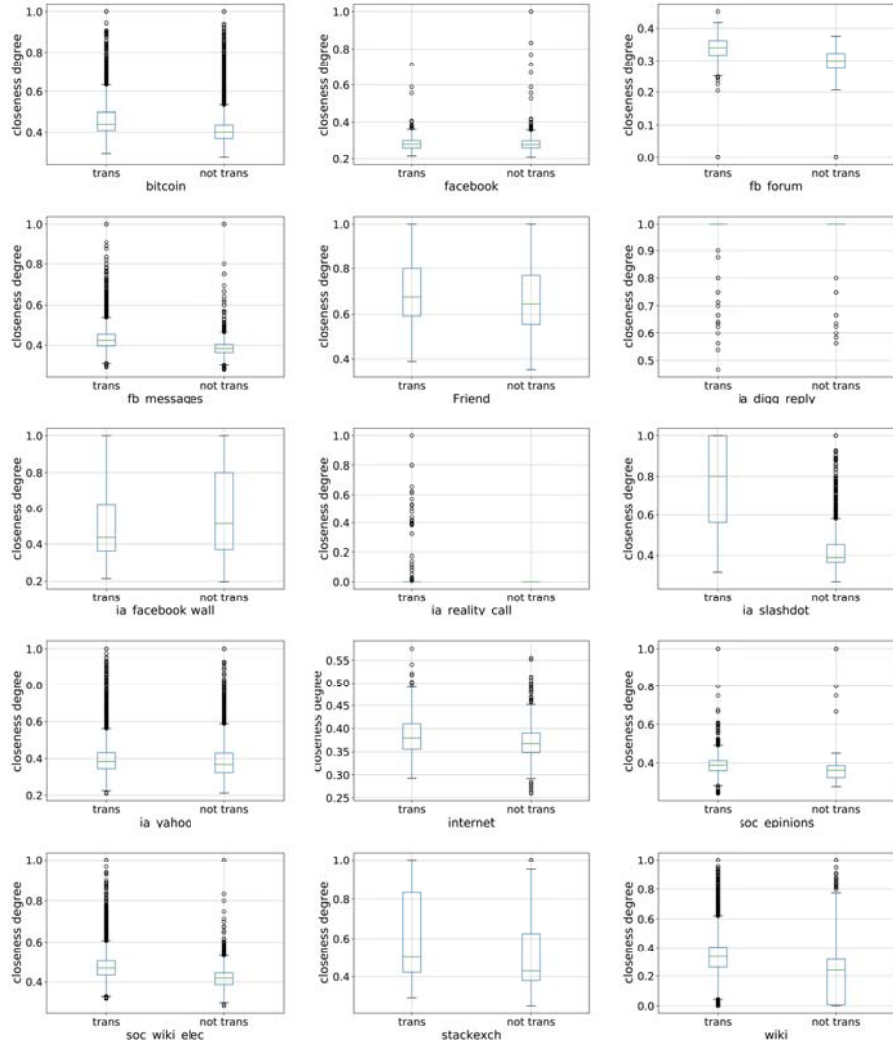


Figure 8: Bitmaps of nodes closeness centrality on 15 data sets

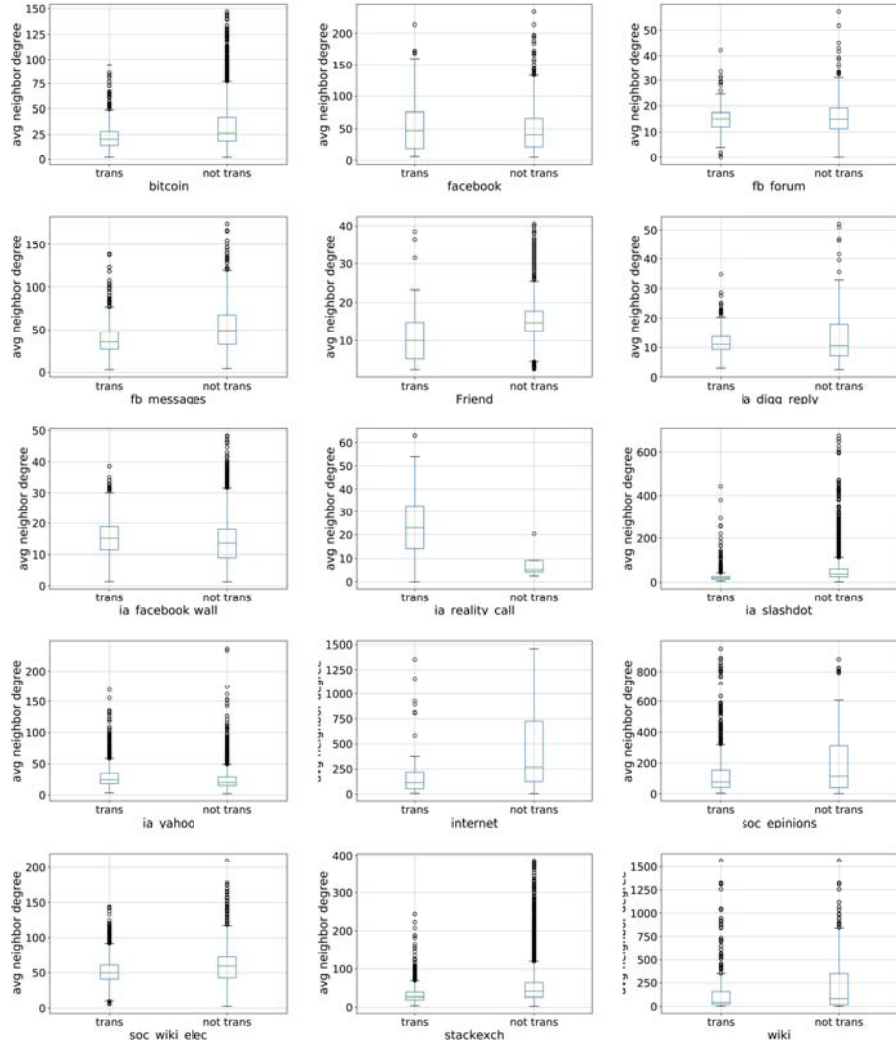


Figure 9: Bitmaps of nodes average neighbor degree on 15 data sets. 1 in x-axis represents the bitmap of nodes transferring their communities, and 0 otherwise.

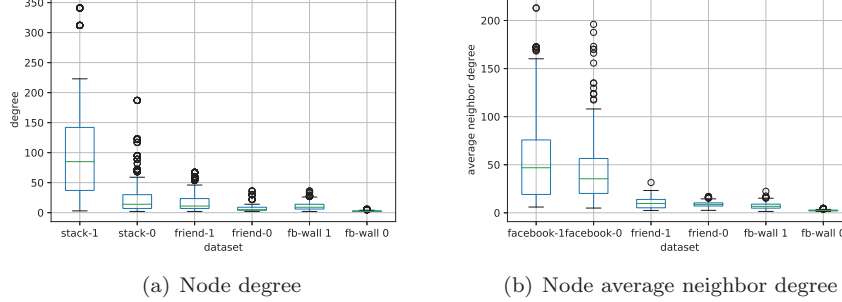


Figure 10: Quartile map of node degree and node average neighbor degree in three data sets

5. Case Study

In this section, we use part of the DBLP data [15] to show the impact of node degree and node average neighbor degree on node community transition.

DBLP is a well-studied data set in many research area, especially in complex network analysis. Our data is extracted from DBLP, and it contains the co-authorship information among the papers from 28 conferences over 10 years (1997 – 2007). These conferences cover three main research areas, including data mining, database and machine learning. Moreover, this data set has a ground truth, so we can extract the community membership of nodes without pre-processing this data.

Figure 11 shows the sample of DBLP data in year 2006 – 2007. The text of a node means ‘average neighbor degree-author name’, e.g. ‘4.82- *Shuicheng Yang*’ means this node represents an author *Shuicheng Yang*, and its average neighbor degree is 4.82. And the scale of node represents node degree, i.e. a big node has more friends than a small node. The top two pictures show the influence of average neighbor degree. *Jun Yan*, *Zheng Chen* and *Ning Liu* are working on the database at previous snapshot (top-left), and they all have large average neighbor degree 9.33. They have a big degree friend *Shuicheng Yang* who is working on machine learning. Influenced by *Shuicheng Yang*, in the next snapshot (top-right) *Jun Yan*, *Zheng Chen* and *Ning Liu* change their research interest to machine learning, i.e. they published a paper about machine learning

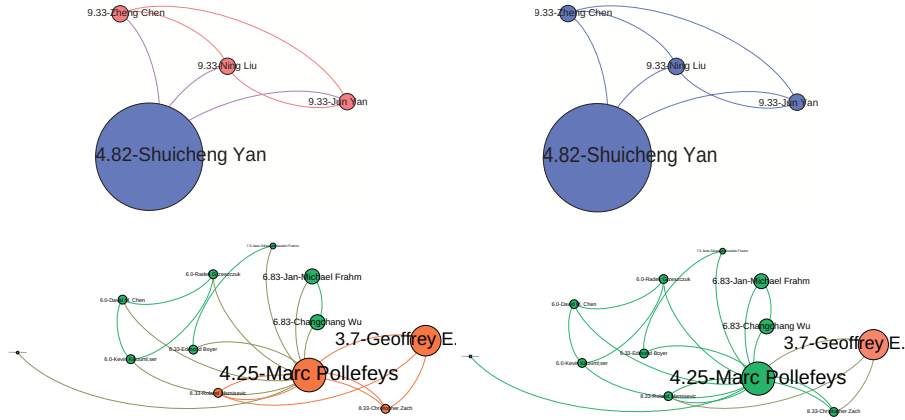


Figure 11: Cases in DBLP shows the influence of node degree and average neighbor degree to node’s community transition.

together in 2006. After investigation, we find that the above four authors jointly
390 published an article on TKDE in 2006¹. And the two pictures at the bottom
show the influence of node degree. *Marc Pollefeys* has a large degree, which
means that he has many friends with this network. Most of his friends are
working on data mining (bottom-left). Influenced by his friends, he changed
his research area to data mining (bottom-right) in the next snapshot. More
395 specifically, *Marc Pollefeys* and one of his friends *Jan-Michael Frahm* published
a paper together on EDGE in 2006². Through these samples, we can intuitively
understand the influence of the node degree and the node average neighbor
degree on the transition of node community. However, more research on the
node average neighbor degree is still needed to explore its impact mechanism
400 on node community transition.

¹Yan, Jun, et al. “Effective and efficient dimensionality reduction for large-scale and streaming data preprocessing.” IEEE transactions on Knowledge and Data Engineering 18.3 (2006): 320-333.

²Sinha, Sudipta N., et al. “GPU-based video feature tracking and matching.” EDGE, workshop on edge computing using new commodity architectures. Vol. 278. 2006.

6. Conclusion

In this paper, we first consider the node’s community transition as a binary classification problem. Through the analysis of 15 real-world dynamic networks, it is found that the degree and average neighbor degree of nodes are the two
405 significant features that affect the pattern of node’s community transition. In fact, we observe that node average neighbor degree is more important than the node degree, which is inconsistent with our previous understanding and also corrects our previous cognition of node transition factors. It has important reference meaning for the generation of dynamic networks and the detection of
410 community structure. We also conduct a case study to explain the insurance against the node degree and node average neighbor degree to node community transition.

Unfortunately, the influence mechanism of the node average neighbor degree on the node community transition has not been found. This is the next step of
415 our work. At the same time, one of the main directions of our future research is how to integrate our results with dynamic community detection methods, which is also what we will do next.

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